Math 141 - Homework 4

Name:

 $Calculate\ the\ following\ limits\ exactly.$

1.
$$\lim_{x \to 0} \frac{1}{2 + \sin x}$$
 2. $\lim_{x \to -1} \frac{2x - 1}{x + 2}$

3.
$$\lim_{x \to 2} \frac{x-2}{x^2 - 2x}$$
4.
$$\lim_{x \to 5} \frac{x^2 - 3x - 10}{x - 5}$$

5.
$$\lim_{x \to 0} \frac{\sin x}{1 + \cos x}$$
 6. $\lim_{h \to 0} \frac{(1+h)^2 - 1}{h}$

7. Find
$$\lim_{h \to 0} \frac{\frac{1}{a(a+h)} - \frac{1}{a^2}}{h}$$
 where *a* is a non-zero constant.

8. Determine the point(s), if any, at which each of the following functions is discontinuous. Classify any discontinuity as jump, removable, infinite, or other.

(a)
$$f(x) = \frac{x}{x^2 - x}$$
 (b) $g(x) = \cot 2x$ (c) $h(t) = t^{-1} + 1$

9. Use the formula $f'(a) = \lim_{x \to a} \frac{f(x) - f(a)}{x - a}$ to find the derivative of $f(x) = x^2$ at a = 3.

10. Expand the polynomial $(x+h)^3$, i.e., multiply the factors (x+h)(x+h)(x+h), then use your answer to find the derivative

$$\frac{d}{dx}x^3 = \lim_{h \to 0} \frac{(x+h)^3 - x^3}{h}$$

11. Use the graph below to find the following derivatives, or explain why they do not exist.



12. Sketch a rough graph of the derivative of the function shown in the graph below. Be sure to include numbers on the x and y-axes.

