

## Midterm 2 Review

## Math 222

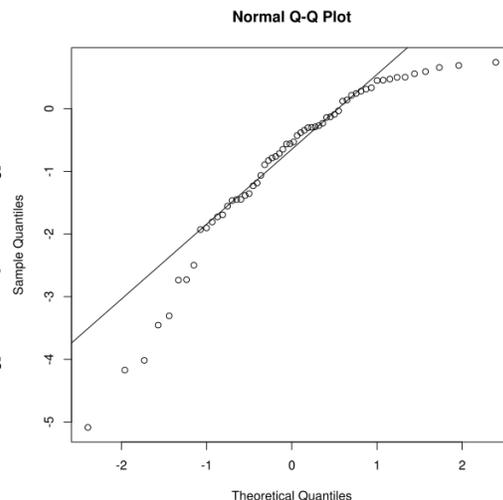
These are problems similar to the ones that might be on midterm 2. Be sure to also review class workshops and problems from the textbook.

1. A news article reports that “Americans have differing views on two potentially inconvenient and invasive practices that airports could implement to uncover potential terrorist attacks.” This news piece was based on a survey conducted among a random sample of 1,137 adults nationwide, interviewed by telephone November 7-10, 2010, where one of the questions on the survey was “Some airports are now using ‘full-body’ digital x-ray machines to electronically screen passengers in airport security lines. Do you think these new x-ray machines should or should not be used at airports?” Below is a summary of responses based on party affiliation.

	Republican	Democrat	Independent	Total
Should	264	299	351	914
Should not	38	55	77	170
Don't know/No answer	16	15	22	53
Total	318	369	450	1137

- (a) Identify the variables in this study.
  - (b) If there was no association between the variables in the study, then what would the expected count be for the number of Republican voters who would say that the new x-ray machines “should not be used”?
  - (c) A chi-squared test for association with the data above has  $\chi^2 = 4.3576$ ,  $df = 4$ ,  $p\text{-value} = 0.3598$ . Explain what that means about the association between the variables.
  - (d) The conclusion of the chi-squared test might be incorrect. If an error was made, was it a Type 1 or a Type 2 Error? Explain.
2. Which option best describes the distribution shown in the normal quantile-quantile plot below?

- A. The distribution is roughly normal.
- B. The distribution is not normal, it is skewed right.
- C. The distribution is not normal, but it is roughly symmetric.
- D. The distribution is not normal, it is skewed left.

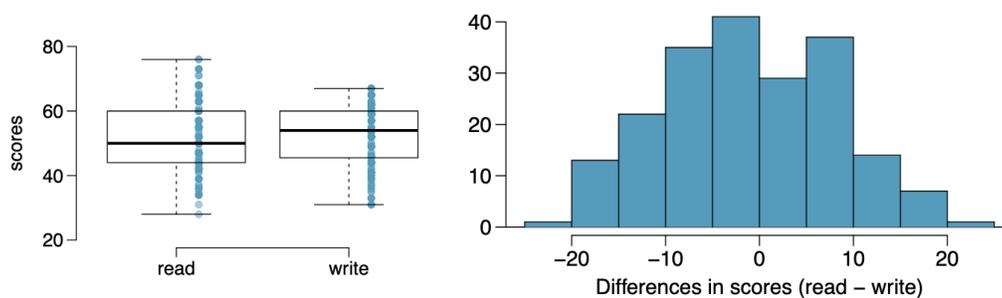


3. Researchers studying the link between prenatal vitamin use and autism surveyed the mothers of a random sample of children aged 24 - 60 months with autism and conducted another separate random sample for children with typical development. The table below shows the number of mothers in each group who did and did not use prenatal vitamins during the three months before pregnancy (periconceptional period).

	Autism	Typical development	Total
No vitamin	111	70	181
Vitamin	143	159	302
Total	254	229	483

- (a) Draw a segmented bar graph that shows the row proportions for the two-way table above (it should have two bars, one for the vitamin group and one for the no vitamin group).
- (b) What are the correct null and alternative hypotheses if we want to see if there is a statistically significant difference between the proportions of kids with autism in the two groups? Use symbols to write the hypotheses.
- (c) The R output of a 2-sample test for proportions with the data above is shown below. As you can see, it includes a 95% confidence interval. Clearly explain what that confidence interval means in this situation.
- ```
## 2-sample test for equality of proportions with continuity correction
##
## data: Autism
## X-squared = 8.3131, df = 1, p-value = 0.003936
## alternative hypothesis: two.sided
## 95 percent confidence interval:
##  0.04475176 0.23474771
## sample estimates:
##   prop 1   prop 2
## 0.6132597 0.4735099
```
- (d) New York Times article reporting on this study was titled “Prenatal Vitamins May Ward Off Autism”. Do you find the title of this article to be appropriate? Explain your answer. Additionally, propose an alternative title.

4. Researchers interested in lead exposure due to car exhaust sampled the blood of 52 police officers subjected to constant inhalation of automobile exhaust fumes while working traffic enforcement in a primarily urban environment. The blood samples of these officers had an average lead concentration of  $124.32 \mu\text{g/l}$  and a SD of  $37.74 \mu\text{g/l}$ ; a previous study of individuals from a nearby suburb, with no history of exposure, found an average blood level concentration of  $35 \mu\text{g/l}$ .
- Write down the hypotheses that would be appropriate for testing if the police officers appear to have been exposed to a higher concentration of lead.
  - Explicitly state and check all conditions necessary for inference on these data.
  - Calculate the one-sample t-value needed to test the hypothesis that the downtown police officers have a higher lead exposure than the group in the previous study.
  - Based on your preceding result, without performing a calculation, would a 95% confidence interval for the average blood concentration level of police officers contain  $35 \mu\text{g/l}$ ?
5. The National Center of Education Statistics conducted a survey of high school seniors, collecting test data on reading, writing, and several other subjects. Here we examine a simple random sample of 200 students from this survey. Side-by-side box plots of reading and writing scores as well as a histogram of the differences in scores are shown below.



- Create hypotheses appropriate for the following research question: is there an evident difference in the average scores of students in the reading and writing exam?
- Check the conditions required to complete this test.

- (c) The average observed difference in scores is  $\bar{x}_{\text{read-write}} = -0.545$ , and the standard deviation of the differences is 8.887 points. What is the corresponding  $t$ -value, and how would you use the `pt(t, df)` function in R to compute the corresponding p-value?

- (d) Using the formula  $\bar{x} \pm t^* \sqrt{s^2 + \frac{s^2}{n}}$  to make a 95% prediction interval with this data, we get a range from  $-18.1$  to  $17.0$ . What are we 95% sure will be between these two numbers?

6. (6 points) In each of the following scenarios, determine whether it would be better to treat the data as matched pairs or as two separate samples.

- (a) We would like to know if Intel's stock and Southwest Airlines' stock have similar rates of return. To find out, we take a random sample of 50 days, and record Intel's and Southwest's share price on those same days.

- (b) We randomly sample 50 items from Target stores and note the price for each. Then we visit Walmart and collect the price for each of those same 50 items.

- (c) A school board would like to determine whether there is a difference in average SAT scores for students at one high school versus another high school in the district. To check, they take a simple random sample of 100 students from each high school.

7. A medical research group is recruiting people to complete short surveys about their medical history. For example, one survey asks for information on a person's family history in regards to cancer. Another survey asks about what topics were discussed during the person's last visit to a hospital. So far, as people sign up, they complete an average of just 4 surveys, and the standard deviation of the number of surveys is about 2.2. The research group wants to try a new interface that they think will encourage new enrollees to complete more surveys, where they will randomize each enrollee to either get the new interface or the current interface. The researchers are hoping that the new interface will increase the average number of completed surveys from 4 to 4.5.

(a) If the researchers enroll  $n$  people to get the new interface and another  $n$  people to get the old interface, then what R command would give the threshold for the two sample  $z$ -value

$$z = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

to be statistically significant at the 5% level?

(b) If the answer to the last part is stored in a variable called `threshold`, then what R command can we use to find the power of the statistical test above (assuming a 1-sided alternative hypothesis, and an effect size of 0.5 extra surveys completed on average with the new interface)?

8. A study of Canadian hockey players found that professional hockey players were far more likely to have birth months early in the year than later in the year. Here is the data from players in the Western Hockey League in 1987.

| Birth Month | Jan to Mar | Apr to Jun | Jul to Sep | Oct to Dec | Total |
|-------------|------------|------------|------------|------------|-------|
| Count       | 84         | 77         | 35         | 34         | 230   |

(a) What statistical test would you do to see if there is a statistically significant difference in the birth months of hockey players than random chance alone would predict?

(b) What are the correct null and alternative hypotheses for this test?

(c) How many of the 230 players would you have expected to be born in each of the four categories if birthdates of hockey players were evenly distributed on the calendar?